Evidence that Psychopathology Symptom Networks do not Replicate

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Abstract

Network analysis is quickly gaining popularity in psychopathology research as a method that aims to reveal causal relationships among individual symptoms. To date, four main types of psychopathology networks have been proposed: (1) association networks, (2) regularized concentration networks, (3) relative importance networks, and (4) directed acyclic graphs. We examined the replicability of these analyses based on symptoms of major depression and generalized anxiety between and within two highly similar epidemiological samples (i.e., the National Comorbidity Survey – Replication \( n = 9282 \) and the National Survey of Mental Health and Wellbeing \( n = 8841 \)). While association networks were stable, the three other types of network analysis (i.e., the conditional independence networks) had poor replicability between and within methods and samples. The detailed aspects of the models—such as the estimation of specific edges and the centrality of individual nodes—were particularly unstable. For example, half of the symptoms were estimated as the “most influential” on at least one centrality index across the six conditional independence networks in the full samples, and only 6–15% of the edges were consistently estimated across these networks. One of the likely reasons for the instability of the networks is the predominance of measurement error in the assessment of individual symptoms. We discuss the implications of these findings for the growing field of psychopathology network research, and conclude that novel results originating from psychopathology networks should be held to higher standards of evidence before they are ready for dissemination or implementation in the field.

Key words: Network analysis; psychopathology; causal inference; psychopathology networks; replication crisis.
**General Scientific Summary:** A statistical method called network analysis is quickly gaining popularity for analyzing the relationships between symptoms of mental disorders. This study found that popular network analysis methods produce unreliable results, particularly for the symptom-level aspects of the models. We highlight the need to be particularly cautious in interpreting, disseminating, or implementing results that arise from psychopathology networks.
Evidence that Psychopathology Symptom Networks do not Replicate

The popularity of network analysis is spreading quickly in the study of psychopathology. In particular, a growing number of studies using cross-sectional analyses of networks of psychopathology symptoms have appeared in the literature since Cramer et al. (2010a) proposed this approach. These networks are based on the foundational premise that psychopathology symptoms causally influence one another as part of a complex dynamical system, thereby contributing to disorder onset and maintenance (Borsboom & Cramer, 2013; Cramer et al., 2010a). Such analyses represent an effort to map the causal structure of symptom-to-symptom relationships within and between traditionally-defined mental disorders (Borsboom & Cramer, 2013; Cramer et al., 2010a).

The proliferation of network analysis is no doubt related to the attractive qualities of the method. For example, network models are promoted as a window into the nuanced and complex dynamic processes of mental disorders; by focusing on observed symptoms, the models appeal to the salience of proximal, observable clinical targets that other statistical techniques may seem distant from. Network analysis is also an accessible statistical method. Borsboom and Cramer (2013) highlighted that “…the application of network models does not require extensive prior knowledge, as many other methodologies do: All one needs is a set of elements and an idea of how these elements are connected.” (p. 100).

Perhaps the most attractive features of network analysis are the graphical representations of the networks, which can display the interrelationships among hundreds of variables in a single figure (e.g., Boschloo, Schoevers, van Borkulo, Borsboom & Oldehinkel, 2016a; Boschloo et al., 2015). Each network figure is generally comprised of circular nodes, which represent the symptoms being analyzed, and linear edges, which represent a pairwise statistical relationship between each pair of nodes. Edges can be weighted (the width of the edge represents the strength of a relationship) or unweighted (representing the presence or
absence of a relationship); directed (unidirectional, indicated with an arrow) or undirected (bidirectional, typically indicated with a line); and positive (e.g., green) or negative (e.g., red). This intuitive interpretation is further facilitated by the Fruchterman and Reingold (1991) algorithm used in many psychopathology network figures, in which strongly related symptoms are attracted towards one another (i.e., tend to cluster together) and symptoms with weaker interrelationships repel one another (i.e., tend to be positioned on the edges of the network).

The Four Main Types of Psychopathology Networks

There are four main types of networks that psychopathologists have used in cross-sectional, observational symptom data, each of which is presented as a step towards characterizing the causal system within and/or between mental disorders (e.g., Borsboom & Cramer, 2013; McNally, 2016). These four types of networks, in turn, can be considered separately based on whether they represent zero-order relationships (e.g., Pearson correlations), or relationships that are conditionally independent of other relationships in the network (e.g., partial correlations).

Association Networks

First, association networks are based on the zero-order bivariate relationships (e.g., Pearson correlations) among the nodes, and include undirected weighted edges to represent the strength of these relationships. Association network figures are useful for visualizing the multivariate relationships among symptoms (Epskamp, Kruis & Marsman, under review-b), and highlight the patterns in which symptoms tend to cluster together (Borsboom & Cramer, 2013). However, association networks do not account for the fact that the correlation between a pair of nodes might be due to their shared relationships with other symptoms (i.e., they may only be conditionally dependent, Borsboom & Cramer, 2013; McNally et al., 2014).

Conditionally Independent Networks
In contrast, the three other main types of psychopathology networks exclude the variance that is shared by more than two symptoms to isolate the *conditionally independent* relationships between each pair of nodes. We will refer collectively to networks based on patterns of conditionally independent relationships (i.e., *concentration networks*, *relative importance networks*, and *directed acyclic graphs*, discussed in more detail below) as *conditional independence networks*. Figure 1 briefly illustrates the difference between conditionally dependent and conditionally independent relationships. For example, on the left of the figure, a large proportion of the relationship between A and B is conditionally dependent on (i.e., overlapping with) C and D. On the right of the figure, we can see the conditionally independent relationship between A and B (i.e., the relationship that is shared between A and B, but unshared with any other symptoms). In the network literature, conditionally independent relationships are purported to “provide clues about the causal skeleton of a network” (Borsboom & Cramer, 2013, p. 105), in that they highlight the direct (versus indirect) relationship between nodes (Robinaugh, LeBlanc, Vuletich & McNally, 2014). In Figure 1, nodes A and B would be more strongly related in an association network than in a conditional independence network, but the smaller conditionally independent relationship between them might be used to infer that they are directly causally related. However, it is important to note that this relationship might also be due to shared item content, a reciprocal effect, or the common effect of an unmodelled variable (Costantini et al., 2015).

As mentioned above, there are three main categories of conditional independence networks that we will explore in this study: *concentration networks*, *relative importance networks*, and *directed acyclic graphs* (DAGs). Concentration networks are made up of undirected weighted edges that represent the conditionally independent relationships between nodes (e.g., partial correlations; see Lauritzen, 1996; van Borkulo et al., 2014a for details).
Concentration networks are often *regularized* to eliminate weak and unreliable estimated edges from the model (see Friedman, Hastie, & Tibshirani, 2008; Tibshirani, 1996 for details). Regularization thus maximizes specificity, but at the cost of sensitivity (Epskamp et al., under review-b); van Borkulo et al. (2014a) suggested that by using a regularization method in binary data “the important connections are almost always correctly identified” (p. 2) and “there is a near absence of false positive among estimated network connections” (p. 3). This purported reliability—and consequent expected replicability—of regularized models is emphasized in the literature (e.g., Boschloo et al., 2016a; Costantini et al., 2015; Epskamp et al., under review-b).

Relative importance networks represent the strength and direction of each edge based on the average amount of variance that, for example, node X predicts in node Y (X → Y), and vice versa (Y → X), after controlling for all possible combinations of the other nodes in the network. In other words, each weighted and directed edge represents the proportion of explained variance (expressed as $R^2$, ranging from 0 to 1) that is attributable to each node after accounting for multicollinearity (i.e., the intercorrelations among all of the nodes in a network). The interpretation of relative importance networks emphasizes when one of the edges between a pair of nodes has higher relative importance than the other (see Johnson & LeBreton, 2004 for further discussion of relative importance). When $X \rightarrow Y$ is stronger than $Y \rightarrow X$ network analysts would infer that X directly predicts Y (Hoorelbeke, Marchetti, De Schryver & Koster, 2016; McNally, 2016; McNally et al., 2014; Robinaugh et al., 2014).

Finally, DAGs aspire to discern causality via constraint-based (e.g., Borsboom & Cramer, 2013) or Bayesian network analysis (e.g., McNally, 2016). More realistically, DAGs depict the direction of probabilistic dependencies so that the unweighted and directed edge $X \rightarrow Y$ indicates that the presence of node X is associated with an increased likelihood that Y will also be present (see Scutari, 2010 for more information on the computation of DAGs).
Recent papers have also emphasized the reliability of DAGs, where “only edges appear that are almost certainly genuine (i.e., ‘false alarm’ edges disappear)” (McNally, 2016, p. 6).

**The Utility of Psychopathology Networks Relies on Generalizability and Replicability**

While the global characteristics of these four types of networks are sometimes interpreted (e.g., the global connectivity and/or density of the network; van Borkulo et al., 2015), it is the detailed features of the networks that are claimed to represent their distinctive promise. Specifically, the proponents of network analysis emphasize two types of utility for psychopathology networks based on cross-sectional symptom-level data. (1) Generating hypotheses about the symptom-to-symptom relationships that characterize trajectories toward the onset and/or maintenance of one or more mental disorders (e.g., Borsboom & Cramer, 2013; Cramer et al., 2010a; Rhemtulla et al., 2016). (2) Identifying the most influential symptoms in the network, which are believed to trigger the development of other symptoms, predict disorder onset, and represent urgent clinical targets (Boschloo, van Borkulo, Borsboom & Schoevers, 2016b; Cramer & Borsboom, 2015; McNally et al., 2014; Rhemtulla et al., 2016). With few exceptions, these detailed characteristics of the networks (i.e., the presence, strength, and/or direction of specific edges; and the centrality of individual nodes) tend to be the focus of network analysis, and form the basis for studies’ conclusions (e.g., Borsboom & Cramer, 2013; Cramer et al., 2010a; Fried et al., 2015; Fried, Epskamp, Nesse, Tuerlinckx & Borsboom, 2016; Rhemtulla et al., 2016).

In short, the aim of network analysis is to characterize the role of individual symptoms in the onset and course of mental disorders. This aim demands that the inferences and hypotheses derived from psychopathology networks are generalizable and replicable beyond the samples in which they were derived. While the proponents of network analysis note that the symptom-to-symptom relationships estimated in a network will not necessarily be present in all individuals (e.g., Cramer et al., 2010a), networks derived from between-
subjects associations would presumably need to be replicable (i.e., in other samples) in order for psychopathology network research to have utility. Replicability is particularly pertinent given that psychology, as a field, is in the midst of a replication crisis (Open Science Collaboration, 2015). This may be at least partly due to a focus on generating new and exciting findings at the expense of rigorous and repeated testing of hypotheses. Inferences made from psychopathology networks are likely to be particularly susceptible to this pitfall, as network analyses are exploratory, data-driven techniques that entail estimation of a large number of parameters. For example, an association or concentration network of posttraumatic stress disorder (PTSD) symptoms from *Diagnostic and Statistical Manual of Mental Disorders – Fifth Edition* (American Psychiatric Association, 2013) would have 20 nodes and 190 possible edges (calculated as $k\times (k-1)/2$, where $k$ is the number of nodes).

There are numerous other harbingers of poor replicability for psychopathology networks, the most salient of which is the inevitable presence of substantial measurement error in symptom-level psychopathology data. In most psychometric models, each of the observed scores for symptoms A to D in Figure 1 comprises *true score* (i.e., the information we are interested in learning more about), *systematic error* (e.g., from overlap in the content of the questions about each symptom), and *random error* (or *noise*). From a psychometric perspective, the most reliable information from the symptoms is in their overlap. For example, the darkest areas of the variance used to estimate association networks in Figure 1 (i.e., the areas with the most overlap) would likely be comprised mostly of *true score* and some *systematic error*. However, the conditionally independent relationships—on the right of Figure 1—are based on the variance shared by only two symptoms, and the reliable variance shared by more than two symptoms is not used to estimate the conditional independence networks. This means that the conditionally independent relationships are more likely to be made up of *systematic error* and *noise*, which makes them vulnerable to subtle changes in the
data and likely to vary depending on the nodes that are included or excluded from an analysis (see Supplementary Materials Appendix S1 for examples that illustrate the sensitivity of conditionally independent relationships to different types of change). Combined with the inherently exploratory nature of psychopathology networks, the large number of parameters estimated, and the emphasis on conditionally independent relationships among symptoms, this means that the networks are likely highly influenced by noise and prone to overfitting the data, potentially resulting in nonreplicable solutions. Our aim herein is to explore this possibility explicitly and empirically.

In line with theoretical reasons to expect poor replicability, there have been multiple studies that have estimated concentration networks of depression, each of which has differed in the rank-orders of node strength centrality (e.g., Fried et al., 2016; van Borkulo et al., 2014a; van Borkulo et al., 2015). The network structure of depression also appears to change depending on the symptoms included in the model, as well as whether it is modelled alone or alongside other syndromes (e.g., Boschloo et al., 2016b; Boschloo et al., 2015; Fried et al., 2016; Robinaugh et al., 2014; van Borkulo et al., 2014a; van Borkulo et al., 2015), although this may be related in part to the use of different measures of depression (Fried, van Borkulo, Cramer, Boschloo, Schoevers, & Borsboom, under review). Similarly, studies that have examined the network structure of posttraumatic stress disorder (PTSD) using each of the four main types of network analysis across two data sets have found results that suggest the different methods uncover different relationships, some of which may represent idiosyncrasies unique to a dataset that do not generalize to other data (McNally, 2016; McNally et al., 2014).

However, despite the *a priori* reasons to expect poor replicability, and the preliminary evidence in extant research that psychopathology network results are unstable, the replicability of the focal characteristics of networks (e.g., the presence, strength, and/or
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direction of specific edges; and the centrality of individual nodes) has not been addressed explicitly to date. In the context of the proliferation of psychopathology network research in prestigious journals, it is therefore critical to determine the extent to which psychopathology networks are replicable.

The Present Study

The aim of the present study was to fill this specific gap in the emerging network literature by testing the replicability of key features in each of the four main network models used in cross-sectional psychopathology symptom research. We examined both generalizability of the results (i.e., attempting to produce convergent results in a similar sample; cf. Lykken, 1968) and the stability of the results (i.e., attempting to duplicate findings in methodologically identical samples by comparing random split-halves within samples; cf. Lykken, 1968). The between-samples generalizability of the results is representative of how we might expect the psychopathology network literature to evolve as network analysts ask similar questions in different datasets. While the within-samples tests do not speak directly to the generalizability of psychopathology network results, they quantify the sensitivity of the networks to smaller differences between samples, and ensure that any differences in the between-samples analyses are not unduly biased by idiosyncrasies in the samples we selected (Brandt et al., 2014).

Through a review of the network analysis literature, we found a variety of methods that have been used to compare networks. These methods include visual comparison of network structure (Costantini et al., 2015; Rhemtulla, Fried, Aggen, Tuerlinckx, Kendler, & Borsboom, 2016), comparing global strength between networks (Beard et al., 2016; van Borkulo et al., 2015), using correlations to quantify the overall similarity in estimated edges between networks (Beard et al., 2016; Rhemtulla et al., 2016), comparing the average node centrality between networks (Curtiss & Klemanski, 2016; Fried et al., 2016; van Borkulo et
al., 2015), and visual comparisons of patterns in node centrality indices (Rhemtulla et al., 2016; van Borkulo et al., 2015). Notably, these analyses have not compared individual edge or node characteristics. Given these are the focal features in interpreting networks, there is an evident mismatch in extant network comparison methods and the intended research questions (cf. Anderson & Maxwell, 2016). Further, all of these comparisons have been conducted within samples for different networks, or between different groups of participants; we could not find any examples of cross-sectional psychopathology network research that tested the replicability of their results in a second similar sample. As such, neither the generalizability nor the stability of the focal psychopathology network characteristics have been tested to date, to the best of our knowledge.

In the present study, we therefore systematically tested the similarities and differences in psychopathology network features—from broad (e.g., the level of connectivity in the networks) to specific (e.g., the rank-order of individual nodes)—between and within two epidemiological samples. We started with the major depressive episode (MDE) and generalized anxiety disorder (GAD) symptom data from the National Comorbidity Survey – Replication (NCS-R; Kessler et al., 2004), which has been the focus of two seminal psychopathology network papers (Borsboom & Cramer, 2013; Cramer et al., 2010a). We analyzed this dataset by applying the methods as they are currently applied in the psychopathology network literature. We subsequently sought to replicate these networks in a similar epidemiological sample (i.e., the 2007 Australian National Survey of Mental Health and Wellbeing [NSMHWB]; Slade, Johnston, Oakley Browne, Andrews & Whiteford, 2009) that used the same structured diagnostic interview. We then compared each type of network in ten pairs of random split-halves within each sample.

An auxiliary aim was to examine the consistency among the three types of network models that represent conditionally independent relationships (i.e., concentration networks,
relative importance networks, and DAGs), all of which identify relationships between symptoms that are interpreted as reflecting causal associations (McNally, 2016; McNally et al., 2014). While we would not necessarily expect the global features of these conditional independence networks to be similar (e.g., connectivity or density), it is crucial for the promoted utility of psychopathology networks that there is consistency in the focal characteristics of the networks, such as the most influential node, and the presence or absence of edges that purportedly reflect causal associations at different levels of abstraction.

**Method**

**Samples and Assessment**

The NCS-R and the NSMHWB are both nationally representative household surveys of English speakers in the United States and Australia, respectively. Detailed information on the methodology of these surveys has been reported elsewhere (Kessler et al., 2004; Slade et al., 2009). Recruitment and consent procedures for NCS-R were approved by the Human Subjects Committees of Harvard Medical School and the University of Michigan; the NSMWHB was conducted under the authority of the Census and Statistics Act 1905. Both surveys were based on the World Mental Health Survey Initiative version of the World Health Organization’s Composite International Diagnostic Interview (WMH-CIDI; Kessler & Ustun, 2004). The NCS-R interviews were conducted between February 2001 and April 2003, and the present study includes the 9282 respondents (mean age = 44.7, standard deviation [SD] = 17.50; male = 44.6%) who participated in the core diagnostic assessment. The NSMHWB interviews were conducted between August and December 2007, and the present study includes the 8841 respondents (mean age = 46.4, SD = 18.99; male = 44.5%) who participated in the survey. The average age was higher in NSMHWB, although the effect size was small ($t(17820.20) = -5.95$, $p < .0005$; Cohen’s $d = .09$); there were no differences in the proportions of men and women between the two samples ($\chi^2(1) = 1.68$, $p = .195$; $\varphi = .01$).
The symptoms that were analysed in the present study were derived from the WMH-CIDI algorithms that code each diagnostic criterion for DSM-IV MDE and GAD as present (1) or absent (0), and are the same in both samples (see Table 1). Missing values that arose from the skip structure of the questionnaire were replaced with zeros, in line with Cramer et al. (2010a) and Borsboom and Cramer (2013). All of the analyses were based on the bivariate relationships among the symptoms, and these patterns were the same in both samples; a model that constrained the correlation matrices to be equal in both samples had excellent fit (comparative fit index [CFI] = 1.000, Tucker-Lewis index [TLI] = .999, root mean square error of approximation [RMSEA] = .017, chi-square difference test \( \chi^2_{\text{diff}} \) (171) = 794.80, \( p < .0005 \))\(^1\). In short, we had two representative population samples of similar size and equivalent symptom characteristics that were conducted using the same instructions, procedures, and measures of MDE and GAD symptoms (cf. Brandt et al., 2014). The only \textit{a priori} reason to expect possible differences between the samples was their countries of origin, and this was accounted for by assessing replicability within the samples (i.e., between split-half pairs).

\textbf{Statistical Analysis}

\textit{Computing the Networks}

Borsboom and Cramer (2013) included a tutorial for the network analysis of the MDE and GAD symptoms in NCS-R\(^2\). However, since the publication of Borsboom and Cramer

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\(^1\) A two-factor (MDE and GAD) confirmatory factor analysis with all parameters constrained to be equal between the two samples also had excellent fit (CFI = .999, TLI = .999, RMSEA = .021; \( \chi^2_{\text{diff}} \) (19) = 188.36, \( p < .0005 \)).

\(^2\) We also completed the tutorial in Borsboom and Cramer (2013) with the aim of reproducing the original results based on GAD and MDE in NCS-R. We were able to reproduce the association network from the NCS-R data. However, we were not able to reproduce the DAG, as the PC algorithm in the \textit{R} package \textit{PcAlg} was order-dependent (i.e., influenced by the order in which variables were included in the analyses). The algorithm was updated in 2012 in the new \textit{pcalg} package (Kalisch, Maechler, Colombo, Maathuis & Buehlmann, 2012) to allow for the computation of order-independent DAGs, and the old \textit{PcAlg} package is no
(2013), there have been developments in the methods for the network analysis of binary data
in particular, but also more broadly for network analysis of cross-sectional psychopathology
data (e.g., Costantini et al., 2015; Epskamp, Borsboom & Fried, under review-a; McNally,
2016; van Borkulo et al., 2014a). Our aim in these analyses was to use the most reliable
methods for estimating networks—as presented by the proponents of network analysis—to
maximize their replicability. As such, rather than rely on the methods from the Borsboom and
Cramer (2013) tutorial (e.g., estimating an association network based on Pearson correlations
in binary data), we chose four network models to compare in the NCS-R and NSMHWB data,
following recommendations from the more recent literature (Costantini et al., 2015; Epskamp
et al., under review-a; McNally, 2016; van Borkulo et al., 2014a): (1) association networks
based on tetrachoric correlations, (2) concentration networks based on regularized Ising
models, (3) relative importance networks, and (4) DAGs based on Bayesian network analysis.

**Association networks** were estimated using the R (R Core Team, 2013) package
qgraph (Epskamp, Cramer, Waldorp, Schmittmann & Borsboom, 2012) based on tetrachoric
correlations to represent the bivariate relationships in the data; tetrachoric correlations are
interpreted just like any other correlation coefficient.

**Ising models** were computed to represent the conditionally independent relationships
between nodes. The edges in these models are based on log-linear regression coefficients,
which can be interpreted much like partial correlations; they represent the association
between a pair of nodes after controlling for their relationships with all the other nodes. We
used the eLasso regularization method in the R package IsingFit (van Borkulo, Epskamp &
Robitzsch, 2014b), which applies an $l1$-penalty to the log-linear regression coefficients to
find an optimal balance of sparsity (i.e., having few edges) and goodness of fit of the network
to the data (e.g., van Borkulo et al., 2014a). Following the recommendations of van Borkulo

longer available for use. A DAG computed using a fully order-independent version of the PC
algorithm in the NCS-R data reproduced only 8 of the 37 (21.6%) original paths.
et al. (2014a), we emphasized specificity in these models by encouraging a parsimonious solution; we set the hyperparameter at .25 to penalize models with more parameters and used the “AND-rule” that requires both regression coefficients (e.g., A→B and B→A) to be non-zero for an edge (e.g., A—B) to be included in the network.

**Relative importance networks** were estimated using the *lmg* metric in the *R* package *relaimpo* (Grömping, 2006). Given all 306 possible edges are estimated in this type of network, we highlighted nodes with higher relative importance by only retaining an edge in the network if it accounted for at least 5% of the variance in the predicted node (cf. Robinaugh et al., 2014) and if it had higher relative importance in a pair of nodes (i.e., accounted for at least .5% more variance than the other edge in the pair). In other words, if A→B had an edge weight of .08 (*R*^2^ = 8%) and B→A had an edge weight of .06 (*R*^2^ = 6%), the network only included the edge from A→B. This was done to facilitate the objective interpretation and comparison of the networks without relying on visual assessment of line weights (cf. Diaconis, 1985). The full uncensored relative importance networks with all 306 edges are included in the Supplementary Materials (Figure S1).

**DAGs** were computed based on Bayesian network analyses (i.e., the hill-climbing algorithm from the *R* package *bnlearn*; Scutari, 2010), as described in McNally (2016). Edges were included in the model if they were present in 85% or more of the permutations. The DAGs were plotted as trees that position predictors upstream from the nodes they predict (i.e., all edges are downward-pointing arrows). All other network figures were plotted in using the Fruchterman and Reingold (1991) algorithm, which positions nodes with stronger connections near the center of the network, and those with weaker connections near the periphery. A Fruchterman and Reingold plot of the DAGs is also available in the Supplementary Materials.

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3 This value was guided by the range of absolute differences between each pair of edges when at least one edge weight was greater than .05. In NCS-R, the range in the absolute values of the difference in edge weights in these pairs was .0001–.0618, with a median of .0062. In NSMHWB the range was .0001–.0659, with a median of .0057.
Supplementary Materials (Figure S2) for consistency.

**Comparing the Networks**

For the between-samples analyses, we treated the NCS-R as the baseline model, and the NSMHWB as the replication model. These analyses tested the generalizability of the results by making comparisons *within* each of the four types of network analysis *between* the two samples (e.g., comparing the Ising model in NCS-R to the Ising model in NSMHWB) as detailed below. The figures of these networks are presented to show examples of each type of network, and to illustrate specific inferences that generalize (or do not generalize) from one network to the other. The within-samples analyses were based on comparisons *within* each type of network and *within* each sample by comparing ten pairs of random split-halves in each dataset. Rather than presenting all twenty sets of analyses, we summarize the results based on the central tendency (median) for each set of split-halves. Reliability within each sample would ordinarily be required before examining reliability between the samples, but in this case presenting both sets of results allowed us to illustrate the ways in which different indicators of replicability vary within and between samples, providing a more complete picture of the performance of network models in cross-sectional symptom-level data.

There are no established methods for systematically comparing the range of network characteristics of interest in psychopathology research or assessing model fit for the four types of networks estimated in this study, to the best of our knowledge. As such, we have carefully defined the effects that we intended to replicate, and tests specific to those effects (cf. Brandt et al., 2014). We compared the network features—from broad to specific—using metrics with varying levels of sensitivity to instability in the network characteristics that are focused on in the psychopathology network literature. Specifically, we compared the

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4 It was immediately evident that the placement of individual nodes and their proximity to one another was unreliable (i.e., differed substantially between networks and was not consistent with node centrality indices), so we did not interpret these features of the networks. This is revisited in the discussion.
following characteristics—presented in order of expected sensitivity to differences between networks:

1) The differences in the global connectivity (i.e., the number of connections that were estimated to be non-zero; Boschloo et al., 2016a; Costantini et al., 2015; Fried et al., 2016) and density (i.e., average edge strength in weighted networks; De Schryver, Vindevogel, Rasmussen & Cramer, 2015) between the networks.

2) Changes in estimated edges, including:
   a. The proportion of edges in the baseline network that replicated,
   b. The average absolute differences (% change) of the replicated edge weights,
   c. The proportion of edges unique to the baseline network (i.e., that failed to replicate), and
   d. The proportion of edges unique to the replication network.

3) The rank-order of the node centrality indices in each network, and consistency in the most central node\(^5\) based on:
   a. **Strength**, which represents the sum of the edge weights connected to a node.
      When edges are unweighted (e.g., in DAGs), this metric is called *degree* and represents the number of edges connected to a node. Similarly, in networks with directed edges, these metrics are presented as *out strength/out degree* and *in strength/in degree* to separate edges that represent \(A \rightarrow B\) (contributing to *out strength* for A) from edges that represent \(B \rightarrow A\) (contributing to *in strength* for A).
   b. **Closeness**, which represents the inverse of the average shortest path length (i.e., the average number of steps in the shortest path between pairs of symptoms) for a given node with all other nodes in the network.

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\(^5\) The most central node was defined as the highest-ranking node for at least two of the three indices (cf. van Borkulo et al., 2014a).
c. *Betweenness*, which represents the number of times a node lies on the shortest path between two other nodes.

The rank-orders of the node centrality indices for each model were compared using Kendall’s tau-b coefficient, as well as matches in rank-order. While tau summarizes the similarities of the relative node rank-orders, examining the exact matches in rank-order (e.g., whether a symptom is ranked first for *strength* in both samples) is more consistent with the way node centrality indices are interpreted in the psychopathology network literature, which focuses on which specific symptom is ranked first, second, third, or last on each centrality index (e.g., Boschloo et al., 2016b; Cramer & Borsboom, 2015; McNally et al., 2014; Rhemtulla et al., 2016). We calculated the matches in node centrality rank-order by sorting the nodes from highest centrality to lowest centrality within each index, and counting the number of nodes with the same rank-order (e.g., fifth) in both samples. Because duplicate values (i.e., tied ranks) were common within each centrality index, nodes were often able to have multiple ranks; for example, if the second, third, and fourth highest centrality values were equal, then the nodes with these values have interchangeable ranks. We took this flexibility in the ranks into account, and counted a match in rank-order if there was any possible order that facilitated a match *and* maintained the sorting from highest to lowest centrality. In other words, we report the maximum possible number of matches in node centrality rank-order.

After doing these comparisons for each pair of networks between and within the two samples, we also briefly examined the overall consistency in estimated edges and node centrality between the conditional independence networks in the full samples. The results are summarized below, and elaborated with specific examples in the discussion.

**Results**

**Tetrachoric Correlation Association Networks**
Tables 2-4 show the results from the network comparisons between the samples and between the split-halves within the samples. The NCS-R and NSMHWB association networks are shown in Figure 2. The darker and thicker edges show that the symptoms of MDE and GAD are intercorrelated more strongly within each disorder, compared to between the disorders, in both examples. All paths were estimated in all of the association networks, which meant their connectivity was identical and all edges were replicated between and within the samples. The density of the networks and the mean differences in edge weights were more similar within the samples than between them, reflecting the greater similarity in the underlying correlation matrices \(^6\). However, this greater similarity in estimated edges was not reflected in node centrality. The node centrality rank-orders tended to be very similar within and between samples; the rank-order correlations ranged from \(\tau = .67\) to \(\tau = .79\), but individual nodes rarely had the same rank when comparing networks within and between samples (13.9–27.8% matches in rank-order). Similarly, the NCS-R and NSMHWB networks had different most central nodes, and the split-half pairs within samples had different most central nodes in 70–80% of cases.

**Regularized Ising Models**

The NCS-R and NSMHWB Ising models are shown in Figure 3. The regularization of the log-linear paths between the nodes has resulted in fewer edges being included in each network, but we can still see distinct MDE and GAD clusters in both networks. The replicability of the edges in the Ising models was remarkably similar between and within

\(^6\) Constraining the correlation matrices to be held equal between each pair of split-halves was consistent with near-perfect model fit in both samples. In NCS-R, all split-half pairs had CFI s and TLI s of 1.000 when constrained to be equal; RMSEA ranged from 0–.011 (all \(ps = 1.000\)); eight of the ten split-half pairs had non-significant chi-square difference tests, and two pairs had small but significant chi-square differences at \(p < .05\); \(\chi^2\) range (171) = 145.45–267.49 (median = 165.12), \(p_{\text{range}} = .000–.892\) (median = .605). In NSMHWB, all split-halves had CFI s and TLI s of 1.000 when constrained to be equal; RMSEA ranged from 0–.005 (all \(ps = 1.000\)); and none of the split-halves were significantly different: \(\chi^2\) range (171) = 148.94–192.18 (median = 156.84), \(p_{\text{range}} = .128–.887\) (median = .764).
samples (see Tables 2–4). For example, the connectivity, density, and proportion of replicated edges were consistent. A large proportion of edges tended to replicate (83.4–86.6%), but these replicated edges differed substantially (i.e., by 30.4–48.4%) in their estimated strength. Node centrality was more idiosyncratic: NCS-R and NSMHWB had different most central nodes, as did all of the split-halves in NSMHWB. In contrast, depressed mood (depr) was consistently estimated as the most central node in NCS-R, such that 80% of the split-half pairs matched. The node centrality rank-order correlations ranged from $\tau = .57$ to $\tau = .80$ between and within samples, but only half of the individual nodes had matches in their rank-order for betweenness centrality (50–55.6% matches in rank-order) and even fewer had matches in their rank-order for strength and closeness centrality (16.7–33.3% matches in rank-order).

**Relative Importance Networks**

The censored relative importance networks estimated in NCS-R and NSMHWB are shown in Figure 4. Neither network had bridging edges between MDE and GAD with edge weights over .05, resulting in distinct disorder clusters. While depressed mood (depr) appears to have a similar role in both networks, there are marked differences between the GAD clusters that are at odds with the similar number of connections and density between the two networks (see Table 2). This similar connectivity and density was also seen between the split-half pairs within each sample, and the replicated edges tended to have similar strength between and within the samples too (see Tables 3 and 4). However, the replicability between samples was worse than within samples, as 25.8% of the edges failed to replicate between samples (versus 6.6–14.6% within samples), and the node centrality rank-orders also varied more between samples. For example, sleep problems in MDE (mSle) was the most central node in NSMHWB, but did not rank in the top three most central nodes on any index in NCS-R.
Directed Acyclic Graphs

Of the four types of network models analysed, the DAGs had the clearest inconsistencies between and within samples (Tables 2–4). For example, by colour-coding the nodes in Figure 5 (GAD in blue and MDE in red; see article online for color, or Table 1 to interpret the symptom abbreviations by disorder) we can see a critical difference between the NCS-R and NSMHWB networks: The NCS-R network has an alternating pattern wherein the core GAD diagnostic criteria predict many of the MDE symptoms, which predict the physiological symptoms of GAD in turn, and nearly all of the symptoms converge in predicting self-reproach (repr). In contrast, in the NSMHWB network nearly all symptoms of GAD—with the sole exception of control over anxiety (ctrl)—precede MDE in the putative causal structure. Further, despite the substantially larger number of estimated edges in NSMHWB, 19.6% of the NCS-R edges still failed to replicate, and the NSMHWB DAG had 37 unique edges (42.1% of the edges in NSMHWB) that were not included in the NCS-R DAG. Node centrality was mixed. For example, out degree had more matches in rank-order than the strength family of centrality indices in other networks, likely due to the compressed information (count vs. continuous scale) in in degree and out degree centrality indices compared to the strength centrality indices in other networks.

Remarkably, the replicability in the split-half pairs within each sample was substantially worse (see Tables 3 and 4). While the connectivity was more similar within versus between samples, a median of only 36.3–52.9% of edges replicated between split-halves. Further, the rank-order correlations and matches in rank-order for node centrality were substantially worse, and only one of the twenty pairs of split-halves had the same most central node.

Consistency between the Conditional Independence Networks
As a follow-up, we briefly examined the consistency in the focal network characteristics (i.e., the most central node, and the presence or absence of specific edges) between the conditional independence networks in NCS-R and NSMHWB. There was very little consistency in the networks. For example, half of the nodes \((n = 9; 50.0\%)\) were ranked as “the most influential” on at least one centrality index (excluding \textit{in strength} and \textit{in degree}) in at least one of the networks, and there was no overlap between the three methods (i.e., no node was ranked highest on a centrality index in the Ising models, relative importance networks, and DAGs). The most striking example of inconsistency between the networks was in the proportion of edges that failed to replicate across all six networks: There were 87 unique undirected edges between the two Ising models, and 28 additional unique directed edges estimated in the relative importance networks and DAGs, giving a total of 115 edges estimated with the aim of uncovering the causal relationships among the 18 symptoms. In comparing the networks, we allowed an undirected edge to be replicated by a directed edge between the same two nodes, and vice versa. Only seven edges (6.1\%) were estimated in all six networks. Comparing the three conditional independence networks within the NCS-R dataset, only 14 of the 96 unique edges (14.6\%) were consistently estimated; within the NSMHWB dataset only 13 of the 112 unique edges (11.6\%) were consistently estimated.\(^7\)

**Discussion**

This aim of this study was to test the generalizability and stability of the four main types of psychopathology symptom network models used in cross-sectional research. Broadly, the global characteristics of the models—such as the presence of MDE and GAD clusters, and the connectivity and density of the networks—tended to be consistent within each

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\(^7\) Given the relative importance networks were highly censored based on arbitrary criteria, we also examined the consistency between the Ising models and the DAGs separately. Across the two samples, there were 114 edges estimated between these four networks, and 29 (25.4\%) were estimated in all four. Within the NCS-R data, 41 (43.2\%) of the edges were estimated in both the Ising model and the DAG; and within the NSMHWB data, 50 (45.0\%) of the edges were estimated in both the Ising model and the DAG.
method between and within the two samples. In contrast, the detailed aspects of the models were much less replicable. Specifically, the three types of models based on patterns of conditional independence among the nodes were generally not consistent between or within the samples with respect to the estimated edges, the rank-order of node centrality, or the most central nodes. This meant that each psychopathology network would result in fundamentally different conclusions regarding the pathways to disorder onset and comorbidity, and regarding which symptoms represent urgent clinical targets, as explored below. Examples of poor and absent replicability are elucidated below and interpreted in the context of the literature. The statistical and theoretical assumptions of the methods that likely account for why we found such poor replicability in the present study are also explored.

Comparing Each Type of Network Between and Within the Two Samples

Tetrachoric Correlation Association Networks

The edges in the association networks were by far the most replicable—between and within samples. This was anticipated, as we would not expect any of the symptom correlations to be exactly zero, which means all of the edges were estimated. However, the node centrality rank-orders were evidently highly sensitive to small—even statistically indistinguishable—differences between networks, as rank-order correlations and matches in individual nodes’ rank-orders in the split-half pairs were generally no more similar than between the full NCS-R and NSMHWB networks.

Another unreliable characteristic in the association networks was the placement of the nodes and their proximity to one another based on the Fruchterman and Reingold (1991) algorithm. Node placement and proximity did not have clear relationships with node centrality, nor with the strength of the relationships among the nodes. For example, the most central nodes in the two full samples (mCon in the NCS-R network and mSle in the NSMHWB network) did not have distinctive positions. It seems likely that this is because the
Fruchterman and Reingold (1991) algorithm not only places strongly connected nodes at the center and weakly connected nodes at the periphery, but also distributes nodes evenly in the network, makes edge lengths uniform, and reflects symmetry in the networks. The position and proximity of nodes in the network are consequently not synonymous with node centrality or influence (cf. De Schryver et al., 2015). Researchers who use this method should be aware that this algorithm may obscure—rather than reveal—the detailed symptom-to-symptom information in a psychopathology network. The Fruchterman and Reingold (1991) algorithm does, however, have utility in revealing more global structural features, such as clusters of interrelated nodes.

**Regularized Ising Models**

The Ising models were the first conditional independence networks we estimated, purportedly representing the “first step” towards determining the causal skeleton of the network (Borsboom & Cramer, 2013, p. 105). One in seven edges tended to fail to replicate between and within the samples, and there was a 30–48% difference in the strengths of the edge weights between each pair of networks. Further, a large proportion of the edges that spanned MDE and GAD (i.e., *bridging edges*) failed to replicate. While these are all substantial changes in the context of a model that is promoted for its specificity (i.e., its ability to detect and exclude false positives from the model, e.g., van Borkulo et al., 2014a), the poor replicability of the bridging edges is of particular concern. From the psychopathology network perspective, these edges represent the pathways to the development of comorbidity between disorders (e.g., Borsboom & Cramer, 2013; Cramer et al., 2010a; Goekoop & Goekoop, 2014; McNally et al., 2014; Robinaugh et al., 2014). As such, the differences in bridging edges between networks would have important implications for the inferences that might be made regarding the development of MDE and GAD and/or

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8 Nearly half (47.4%) of the bridging edges failed to replicate from NCS-R to NSMHWB, and a median of 56.9–69.2% of bridging edges failed to replicate in the split-half pairs.
comorbidity between them. For example, in the full NSMHWB Ising model it might have been inferred—see Borsboom and Cramer (2013)—that chronic worry leads to sleep problems, which lead to fatigue, which leads to depressed mood \((anxi – mSle – mFat – depr)\). This inference cannot be made in the full NCS-R model. Similarly, in the full NCS-R model it might have been inferred that a combination of chronic worry \((anxi)\) and difficulty controlling this worry \((ctrl)\) activates depressed mood \((depr)\), which in turn activates the strongly connected cluster of MDE symptoms \((inte, weig, mSle, mFat, mCon, \text{and } suc)\). This same inference cannot be drawn from the NSMHWB network.

**Relative Importance Networks**

Before interpreting the relative importance networks, it is important to note that our networks were highly censored based on arbitrary criteria for determining relative importance. The full networks each had 684 parameters to interpret and compare (i.e., the weight and direction of each of the 306 edges, and the three centrality indices for each of the 18 nodes), which would be an onerous task to conduct objectively (Diaconis, 1985). This difficulty to objectively identify important results in highly parameterized network models (i.e., to preclude confirmation bias) is a general limitation of all psychopathology networks, which we will revisit later. These uncensored networks had variable replicability\(^9\), but given all edges were estimated and represented small effect sizes (median \(R^2 = 1–2\%\)), the substantive interpretation of the networks tended to be similar.

Overall, the censored relative importance networks tended to have greater replicability within versus between samples, particularly in terms of replicated edges. This was likely due to the censoring of weaker edges, which removed 89–92\% of the estimated edges.

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\(^9\) All edges were estimated in the uncensored relative importance networks, which meant that 100\% of the edges were replicated. The average difference in edge strength between NCS-R and NSMHWB networks was 23.1\%; the most central nodes did not match; node centrality rank-order correlations were similar to the censored networks (\(\tau_{range} = .52–.87\)), but fewer individual nodes had matches in their centrality rank-orders (27.8–50.0\%).
edges from the full networks. Combined with the more similar bivariate relationships between the split-half pairs, the limited focus on only the strongest relationships in the network likely maximized the similarities and stability of the estimated edges. In contrast, the generalizability of the relative importance edges between samples was the poorest of all four types of networks: A quarter of the edges in NCS-R did not replicate, the majority of which were feeling on edge (edge) predicting other GAD symptoms. As was the case for the Ising models, these differences had important implications for the inferences we would make from the two networks. For example, in the NCS-R network, edge had particularly high relative importance for GAD—predicting nearly every other node, and acting as the only link to the three core diagnostic criteria (anxi, even, and ctrl). These results may have led some investigators to emphasize feeling on edge as an “urgent target for clinical intervention” (McNally et al., 2014, p. 10), and press for the development and implementation of clinical interventions to address feeling on edge in GAD. However, these relationships were not present in the NSMHWB network where feeling on edge was of trivial importance, which suggests that those hypothetical efforts to treat the most central symptom in NCS-R would likely have been misguided.

One noteworthy consistency between the NCS-R and NSMHWB relative importance networks was that there were no nodes in the MDE cluster that accounted for more than 5% of the variance in the GAD cluster, and vice versa (i.e., no bridging edges in the censored networks). In the context of the MDE and GAD literature, which highlights the remarkable overlap between the disorders (e.g., Moffitt, Harrington, Caspi, Kim-Cohen, Goldberg, Gregory & Poulton, 2007), this result illustrates the importance of the shared variance between the symptoms for understanding the relationship between disorders. As we indicated in the illustrative example in Figure 1, this shared variance (i.e., the overlap among symptoms) is largely excluded in models that examine patterns of conditionally independent
relationships, including relative importance networks. In contrast, latent variables are estimated based exclusively on shared variance, which is more reliable and less susceptible to small differences in the underlying data than the variance that comprises conditionally independent relationships (see Supplementary Materials Appendix S1). Accordingly, we found a latent variable model of these data (i.e., a two-factor confirmatory factor model) to be highly replicable between the two samples in the present study.

**Directed Acyclic Graphs**

Directed acyclic graphs were the clearest example of poor replicability in the network models we compared. For example, given the number of unique edges in each of the full sample DAGs, there were 48 causal relationships that might be inferred in one of the samples but not the other. Replicability was even worse in the split-half pairs with a median of nearly a half to two-thirds of the edges failing to replicate. This striking lack of replicability highlights the sensitivity of DAGs to small differences in the relationships among symptoms in the network, and is at odds with their purported reliability (e.g., McNally, 2016). In the DAGs based on the full samples, it was clear the difference in estimated edges could potentially lead to two very different inferences: First, in the NCS-R network, that the symptoms of the disorders are inextricably intertwined; second, in the NSMHWB network, that GAD is a precursor to—or causes—MDE. Overall, the lack of stability and generalizability in the DAGs is to be expected once we understand the assumptions, discussed below, that underlie the estimation and interpretability of the models.

**Comparing the Six Conditional Independence Networks**

While there were evidently inconsistencies within each of the network methods, the most apparent discrepancies were between the methods; specifically, between the six networks that represented the patterns of conditional independence in the full data sets. For example, half of the nodes were indicated as the most central by at least one centrality index
across the six conditional independence networks. This reiterates the point that interpreting the most central node in a network as an urgent target for clinical intervention is likely to be a misguided use of time and resources. It also raises the question of how the centrality indices should be interpreted individually, given they are highly sensitive to small differences in the data, and appear to be measuring different constructs rather than converging on particularly important or influential nodes. Ultimately, it is not clear that *betweenness* or *closeness* mean anything in psychopathology research. We would suggest that the move towards relying on the *strength* family of node centrality indices alone (e.g., Boschloo et al., 2016b; Curtiss & Klemanski, 2016; Fried et al., 2016) is a good idea because these indices directly summarize the strength and/or number of bivariate associations for each node.

In addition to the evident discrepancies in the node centrality indices, there was also remarkably low convergence between the conditional independence networks in the estimation of edges. Take, for example, the popular axiom in network analysis “If one does not sleep, one will get tired eventually (insomnia $\rightarrow$ fatigue)” (Borsboom et al., 2016, p. 9), which is often used as a self-evident example of symptom-to-symptom causality to justify the premise of network analysis (e.g., Borsboom & Cramer, 2013; Borsboom et al., 2011a; Borsboom et al., 2016; Cramer & Borsboom, 2015; McNally, 2016; McNally et al., 2014). Between the six full-sample conditional independence networks, there were 40 different edges where this relationship could manifest. It was absent in 80% of cases. In the 20% of cases where it was present, it was estimated in three different places (mSle—mFat, gSle—gFat, and gSle—mFat) across four of the networks, and characterized by a negative relationship in the NCS-R Ising model (gSle—mFat).

Overall, fewer than one in every sixteen of the edges (6%) were consistently estimated across the six conditional independence networks; this proportion rose to 12-15% comparing the networks within each sample. Even in the least restrictive comparison between
conditional independence networks (i.e., comparing only the Ising model and the DAG within the NCS-R or NSMHWB data sets), less than half of the edges were present in both networks. The choice of network model may thus result in vastly different conclusions, which is inconsistent with the way these models are discussed in the psychopathology network literature. These striking dissimilarities between the different types of network analysis underscore the importance of considering the statistical and theoretical underpinnings of each model.

**Why Might Conditional Independence Networks have Such Poor Replicability?**

The inconsistency within and between the conditional independence network analyses raises the question of *why* these methods—which are all intended to represent the causal skeleton of a network—give rise to inconsistent and unstable results. To start, we might consider the question: What are the networks representing, if not robust causal relationships among symptoms? Network analysis research borrows heavily from the language of graph theory to discuss *activation spreading through the networks*, and nodes being *turned on* or *turned off* (e.g., McNally, 2016; McNally et al., 2014; van Borkulo et al., 2014a), but it is not clear what this means in the context of the cross-sectional relationships among symptoms of psychopathology. Ultimately the edges in the networks are visual representations of correlations (association networks), or the combined results of multiple multivariate regressions (Ising models, relative importance models), or the patterns of conditional probabilistic independence among the nodes (DAGs). Reminding ourselves of this reality highlights many of the stumbling blocks in applying network analysis to psychopathology data. Coming back to the statistical and theoretical foundations of network analysis can also offer some clues as to why the networks might be behaving unpredictably, as many of the underlying assumptions of the methods are not met in cross-sectional and observational symptom-level psychopathology data.
Violated Statistical Assumptions

By definition, cross-sectional and observational symptom-level psychopathology data do not have the necessary information to derive causal relationships, nor do they meet the required assumptions. For example, by relying on atemporal, unrandomized, non-experimental data, there is limited causal information in the data to start with (Dawid, 2008; Winer et al., 2016). We are also dealing with “noisy” dynamic systems where a single state (i.e., the presence of any given combination of symptoms) might lead to any number of future states, which further limits causal information (Markon & Jonas, 2016). Trying to draw either casual or directional inferences from cross-sectional data thus relies on strong and strict statistical assumptions (Dawid, 2008; Wiedermann & von Eye, 2015a, 2015b). Further, directionality of the edges in relative importance networks and DAGs cannot be established—not only because of the high likelihood of violating specific statistical assumptions, but because reversing the direction of an edge results in a model in the same equivalence class (i.e., with the same implied covariance matrix), which is typically indistinguishable on the basis of statistical evidence, including the size of the directed effects (Thoemmes, 2015). Most importantly, to avoid making misleading conclusions, there is a fundamental assumption that all nodes that may have a causal role are included in the network (i.e., every common cause that two or more variables share; Dawid, 2008; Glymour, 1997). In psychopathology research, it is unfortunately inevitable that there are external factors with direct and indirect effects on the nodes that have not been modelled (Borsboom, Epskamp, Kievit, Cramer & Schmittmann, 2011b; Young, 2015). Ultimately, psychopathology networks do not and cannot illuminate causal relationships among psychopathology symptoms in cross-sectional data.

Other key statistical pitfalls of psychopathology networks were described earlier: The influence of measurement error in conditional independence networks, the inherently
exploratory nature of the methods, and the estimation of hundreds of parameters in most examples mean that the methods are inherently prone to overfitting the data, resulting in non-replicable solutions. Among the many parameters in each network model, it is easy to identify a few intuitive findings to bolster our confidence in their validity. However, there are no established guidelines with which to evaluate the models or interpret the parameters objectively. This introduces additional error and bias into the interpretation of the results, which is unavoidably tainted by confirmation bias (Diaconis, 1985). We recommend some changes for psychopathology network analysis shortly to address these limitations.

**Violated Theoretical Assumptions**

In addition to the statistical pitfalls of conditional independence networks, the utility of cross-sectional psychopathology networks fundamentally relies on the assumption of *ergodicity*: that the between-person structure at one time is the same as the within-person structure over time (Molenaar, 2004). In contrast with this assumption, the proponents of network analysis expect psychopathology networks to vary over time and individuals (e.g., Borsboom & Cramer, 2013; Borsboom et al., 2011b; Cramer & Borsboom, 2015; Cramer, Waldorp, van der Maas & Borsboom, 2010b; Rhemtulla et al., 2016). Consistent with these expectations, time series network analyses of depression symptoms differ from cross-sectional analyses (Bringmann, Lemmens, Huibers, Borsboom & Tuerlinckx, 2015; Fried et al., 2016), and individuals have been found to have highly distinct networks of associations among domains of psychopathology (Beltz, Wright, Sprague, & Molenaar, 2016; Wright, Beltz, Gates, Molenaar & Simms, 2015). These assumptions evidently require further investigation. However, if intraindividual networks do indeed “differ markedly in terms of their architecture” (Cramer & Borsboom, 2015, p. 5), and are expected to change over time (Cramer et al., 2010b), then it is likely that networks represent ungeneralizable and *locally irrelevant* constructs (Borsboom, Mellenbergh & van Heerden, 2003). In short, it is not clear
how networks derived from between-subjects variation in observational data can have utility in identifying clinically useful information. Borsboom et al. (2003) concluded that “It is clear that between-subjects models do not imply, test, or support causal accounts that are valid at an individual level” (p. 214). This raises a new question: What is the utility of psychopathology networks?

**Redeeming the Utility of Psychopathology Networks**

In the present study we have presented evidence that conditional independence psychopathology networks are unstable and lack replicability, likely due at least in part to the predominance of measurement error in the nodes. It is also evident that psychopathology networks based on cross-sectional observational symptom-level data are not appropriate for making causal inferences. Further, it seems likely that networks derived from between-subjects variation will not generalise to individuals, as discussed above. As such, it is unrealistic to expect that psychopathology networks can fulfil the optimistic expectations surrounding their utility. Specifically, the estimated edges and most central nodes in conditional independence networks are unlikely to represent important dynamic relationships among symptoms, paths to disorder onset and maintenance, or influential symptoms that should be the focus of future clinical interventions. As it stands, the unique utility of network analysis in cross-sectional psychopathology research thus seems limited to visualizing complex multivariate relationships in association networks (remembering not to interpret node placement, proximity, or closeness or betweenness centrality).

**Recommendations to Improve Network Analysis**

The flaws in the current applications of psychopathology networks do not detract from the attractive idea of analyzing symptom-level relationships that might allow us to carve psychopathology at finer joints, thereby deepening our understanding the dynamic mechanisms of disorder onset, maintenance, and treatment (Cramer et al., 2010a; Goekoop &
Goekoop, 2014). As such, it is useful to consider how these methods could be improved to overcome some of the flaws in their current application. The \textit{minimum} change that we would recommend for cross-sectional psychopathology network estimation would be to improve the measurement of symptoms, thus reducing the measurement error modeled in conditional independence networks. One road to this change would be to use multiple items to measure each symptom, and/or to use multiple methods, such as self-report, others’ reports, daily diaries, observation, or physiological measures (cf. Fried & Nesse, 2015). Analyzing broader constructs—such as symptom clusters (e.g., Anker et al., 2017)—versus single symptoms would also be amenable to this approach. Specifically, we would suggest—as others have (Eaton, 2015; Epškamp et al., in press; Markus, 2010; Stapel, 2015; Young, 2015)—that integrating latent variables into network analysis is the best way forward. We echo the suggestions made by Epškamp et al. (in press), who recently proposed \textit{latent network modeling}, in which latent variables are used to extract the most reliable variance from multiple measures of a symptom, and these latent variables subsequently act as the nodes in a network analysis. This method helps to ensure that the conditional independence networks are modeling more true score, rather than error, although it is noteworthy that latent variable models also face challenges inherent in the assessment of psychopathology (e.g., associations among multiple informants are often modest, and multiple ways to approach this issue have been suggested; Bauer et al., 2013; Funder & West, 1993). Taking a hypothesis-driven approach to controlling for the shared variance among symptoms (e.g., Anker et al., 2017) could also avoid the over-partialling of shared variance that currently weakens the replicability of the fully conditionally independent edges. However, it is important to note that even if these changes were made, the other limitations of network analysis will remain.

Other changes to strengthen not only the reliability but the validity of network analysis would include analyzing data that contains more causal information, such as data
with temporal information (e.g., longitudinal or intensive time series data) and experimental or quasi-experimental data (e.g., randomized groups in treatment studies). These changes are routinely recommended in the network analysis literature (Borsboom & Cramer, 2013; Borsboom et al., 2016; Cramer & Borsboom, 2015; Cramer et al., 2010a; Rhemtulla et al., 2016), and would represent a necessary step for these models to live up to their promise. Researchers should also routinely examine the generalizability of findings from psychopathology networks, including the presence, strength and direction of specific edges and the centrality of individual nodes, by replicating them in multiple samples (cf. Klaiber, Epskamp & van der Maas; van Borkulo et al., 2014a). The replicability of networks could also be improved with the continued development of methods to establish confidence intervals for estimated parameters in the four main types of psychopathology networks (cf. Epskamp et al., under review-a).

Further, in contrast to Borsboom and Cramer’s (2013) suggestion that “the application of network models does not require extensive prior knowledge, as many other methodologies do” (p. 100), we emphasize that it is essential that researchers understand and carefully consider the assumptions that underlie these statistical methods. While estimating a network model in R is straightforward and the required code is freely available, the underlying statistics are complex. Researchers should be explicit about justifying and testing the underlying assumptions—including the assumptions for computing the foundational correlation matrices (cf. Cliff, 1996)—and be aware of how sensitive the models can be to violations of these assumptions (Dawid, 2008). Finally, researchers should consider alternative statistical models or methods that might be appropriate for their data, as there are many different statistical models that can fit any given data set, including multiple statistically equivalent models (Dawid, 2008; Epskamp et al., under review-b; Klaiber et al.; Markon & Jonas, 2016). In order for this to become common practice, it is important to
continue to develop methods to rigorously evaluate and compare networks with one another, and with other methods.

Limitations of the Present Study

Much of the present discussion has been focused on the limitations of network analysis in general, as revealed by evidence of limited replicability and consideration of corresponding methodology. However, it is also important to note the specific limitations of the present study as an examination of replicability in network analysis. The primary limitation was that we could not find established methods for comparing the variety of characteristics of interest in psychopathology networks. We were consequently guided by our review of the literature to identify the focal characteristics of psychopathology networks and to determine reasonable ways to compare these characteristics with varying levels of sensitivity to change. Further, our analyses were based on networks of eighteen dichotomous nodes, so we cannot be sure that these findings will generalize to smaller or larger networks, or to other scales of measurement. Similarly, our analyses were based on comparing two samples, and multiple sets of random split-halves within those samples. Other comparisons are possible (e.g., testing generalizability between samples matched and/or differentiated by specific characteristics; quantifying stability in samples with substantial overlap) and we encourage ongoing efforts to evaluate the replicability of network models across other types of sample comparisons. It is also important to note that our discussion emphasized the weaknesses of psychopathology networks, with relatively little emphasis on the examples of replication in the networks. However, the design of the present study was engineered to maximize the replicability of the networks, and the examples of failures to replicate that we elucidated in-text were consistent with the overall trends in the methods. Importantly, the patterns of instability and poor generalizability in the results were evident even in randomly split halves within the two epidemiological samples. We are therefore confident that the
limitations of the present study did not compromise the validity of the results, particularly in the context of the extant literature, which shows that psychopathology networks vary based on the sample, item content, number of constructs included, and specific type of network analysis used.

**Conclusion**

We found psychopathology networks to have poor replicability between and within methods and samples. The more detailed aspects of the models were the least replicable, and this trend was particularly pronounced in the conditional independence networks. This poor replicability likely arises due to the violated statistical and theoretical assumptions that underlie the models, and highlights that these methods—as they are currently applied—have little utility. We look forward to developments in this area that involve building on the fundamentals of latent variable modeling, to improve the measurement of key symptom constructs, and to use designs that are suited to discerning potential fine-grained relationships among symptoms (cf. Epskamp et al., in press). Ultimately, we suggest that novel results originating from psychopathology networks should be held to higher standards of evidence before they are ready for dissemination or implementation in the field.
References


realities require complex theories: Refining and extending the network approach to mental disorders. *Behavioral and Brain Sciences*, 33, 178-193. doi: 10.1017/S0140525X1000920


Table 1. *Abbreviations for Symptoms Included in Analyses*

<table>
<thead>
<tr>
<th>Major Depressive Episode (MDE)</th>
<th>Generalized Anxiety Disorder (GAD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Abbreviation</td>
<td>Symptom</td>
</tr>
<tr>
<td>depr</td>
<td>Depressed mood</td>
</tr>
<tr>
<td>inte</td>
<td>Loss of interest</td>
</tr>
<tr>
<td>weig</td>
<td>Weight problems</td>
</tr>
<tr>
<td>mSle</td>
<td>Sleep problems</td>
</tr>
<tr>
<td>moto</td>
<td>Psychomotor disturbances</td>
</tr>
<tr>
<td>mFat</td>
<td>Fatigue</td>
</tr>
<tr>
<td>repr</td>
<td>Self-reproach</td>
</tr>
<tr>
<td>mCon</td>
<td>Concentration problems</td>
</tr>
<tr>
<td>suic</td>
<td>Suicidal ideation</td>
</tr>
</tbody>
</table>
Table 2. Summary of the Comparisons among the Networks between the National Comorbidity Survey–Replication (NCS-R) and the National Survey of Mental Health and Wellbeing (NSMHWB)

<table>
<thead>
<tr>
<th>Network Characteristics</th>
<th>Association Networks</th>
<th>Regularized Ising Models</th>
<th>Censored Relative Importance Networks</th>
<th>Directed Acyclic Graphs</th>
</tr>
</thead>
<tbody>
<tr>
<td>Comparing Global Characteristics</td>
<td>NCS-R</td>
<td>NSMHWB</td>
<td>NCS-R</td>
<td>NSMHWB</td>
</tr>
<tr>
<td>Connectivity (% possible edges)</td>
<td>153 (100%)</td>
<td>153 (100%)</td>
<td>80 (52.3%)</td>
<td>79 (51.6%)</td>
</tr>
<tr>
<td>Density</td>
<td>0.74</td>
<td>0.79</td>
<td>1.10</td>
<td>1.17</td>
</tr>
</tbody>
</table>

Changes in Estimated Edges

| Mean absolute % change in edge weights of replicated edges | 5.0% | 30.4% | 8.0% | N/A |
| Proportion of edges that replicated from NCS-R to NSMHWB | 153 (100%) | 69 (86.3%) | 23 (74.2%) | 45 (80.4%) |
| Edges that failed to replicate from NCS-R | 0 (0%) | 11 (13.8%) | 8 (25.8%) | 11 (19.6%) |
| Edges unique to NSMHWB | 0 (0%) | 10 (12.7%) | 3 (11.5%) | 37 (42.1%) |

Node Centrality

<table>
<thead>
<tr>
<th>Most central node</th>
<th>NCS-R</th>
<th>NSMHWB</th>
<th>NCS-R</th>
<th>NSMHWB</th>
<th>NCS-R</th>
<th>NSMHWB</th>
<th>NCS-R</th>
<th>NSMHWB</th>
</tr>
</thead>
<tbody>
<tr>
<td>mCon</td>
<td>mSle</td>
<td>depr</td>
<td>anxi</td>
<td>mSle</td>
<td>N/A</td>
<td>anxi</td>
<td>anxi</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Rank-order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strength/Out Strength/Out Degree</td>
<td>.79</td>
<td>4 (22.2%)</td>
<td>.69</td>
<td>3 (16.7%)</td>
<td>.73</td>
<td>6 (33.3%)</td>
<td>.39</td>
<td>12 (66.7%)</td>
</tr>
<tr>
<td>In Strength/In Degree</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
<td>.57</td>
<td>3 (16.7%)</td>
<td>.92</td>
<td>16 (88.9%)</td>
</tr>
<tr>
<td>Closeness</td>
<td>.70</td>
<td>5 (27.8%)</td>
<td>.71</td>
<td>3 (16.7%)</td>
<td>N/A</td>
<td>18 (100%)</td>
<td>1.00</td>
<td>18 (100%)</td>
</tr>
<tr>
<td>Betweenness</td>
<td>N/A</td>
<td>18 (100%)</td>
<td>.77</td>
<td>10 (55.6%)</td>
<td>.46</td>
<td>16 (88.9%)</td>
<td>.34</td>
<td>5 (27.8%)</td>
</tr>
</tbody>
</table>

a No node ranked as most central for at least two centrality indices.
b All of the nodes had an estimated centrality index of 0.
At least 16 (89%) of nodes had an estimated centrality index of 0. 

Note. Tied ranks (i.e., duplicate values) were common within each centrality index, and enabled nodes to have multiple possible ranks; a match was counted if a symptom could have an identical unique rank-order (e.g., fifth) in both samples. Mismatches were only counted if there was no possible combination of rank-orders that simultaneously facilitated a match and maintained a numerically ordered set of values. See Table 1 for node abbreviations.
Table 3. Summary of the Comparisons between the Ten Pairs of Random Split-Halves from the National Comorbidity Survey–Replication; Median (Range)

<table>
<thead>
<tr>
<th>Network Characteristics</th>
<th>Association Networks</th>
<th>Regularized Ising Models</th>
<th>Censored Relative Importance Networks</th>
<th>Directed Acyclic Graphs</th>
</tr>
</thead>
<tbody>
<tr>
<td>Connectivity (% possible edges)</td>
<td>100% (N/A)</td>
<td>100% (N/A)</td>
<td>46.4% (44.4–48.4)</td>
<td>47.1% (45.8–49.7)</td>
</tr>
<tr>
<td>Density (average edge strength)</td>
<td>.74 (.73–.76)</td>
<td>.74 (.72–.75)</td>
<td>1.14 (1.11–1.19)</td>
<td>1.13 (1.10–1.19)</td>
</tr>
</tbody>
</table>

Changes in Estimated Edges

| Mean absolute % change in edge weights of replicated edges | 1.6% (1.0–3.9) | 33.7% (27.7–40.3) | 7.4% (6.1–9.3) | N/A |
| Proportion of edges that replicated from the first random half to the second | 100% (N/A) | 86.6% (81.9–91.4) | 92.0% (81.8–100) | 36.3% (29.1–69.4) |
| Edges that failed to replicate from the first random half | 0% (N/A) | 13.4% (8.6–18.1) | 8.0% (0–18.2) | 63.7% (30.6–70.9) |
| Edges unique to the second random half | 0% (N/A) | 15.4% (9.9–18.1) | 6.8% (0–17.6) | 58.4% (42.6–71.2) |

Node Centrality

<table>
<thead>
<tr>
<th>Same most central node in both split-halves</th>
<th>% matched</th>
<th># most central</th>
<th>% matched</th>
<th># most central</th>
<th>% matched</th>
<th># most central</th>
<th>% matched</th>
<th># most central</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rank-order</td>
<td>Correlation</td>
<td>Matches in Rank-Order</td>
<td>Correlation</td>
<td>Matches in Rank-Order</td>
<td>Correlation</td>
<td>Matches in Rank-Order</td>
<td>Correlation</td>
<td>Matches in Rank-Order</td>
</tr>
<tr>
<td>Strength/ Out Strength/ Out Degree</td>
<td>.79 (.66–.86)</td>
<td>22.2% (0–44.4)</td>
<td>.80 (.63–.87)</td>
<td>27.8% (5.6–50)</td>
<td>.82 (.73–.89)</td>
<td>47.2% (33.3–61.1)</td>
<td>.25 (.02–.62)</td>
<td>36.1% (16.7–55.6)</td>
</tr>
<tr>
<td>In Strength/</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
<td>.76</td>
<td>33.3%</td>
<td>.36</td>
<td>50.0%</td>
</tr>
</tbody>
</table>
### In Degree

<table>
<thead>
<tr>
<th>Centrality Index</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(.57–.83)</td>
<td>(16.7–77.8)</td>
<td>(.23–.62)</td>
</tr>
</tbody>
</table>

### Closeness

<table>
<thead>
<tr>
<th>Centrality Index</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(.54–.80)</td>
<td>(0–27.8)</td>
<td>(.41–.71)</td>
</tr>
</tbody>
</table>

### Betweenness

<table>
<thead>
<tr>
<th>Centrality Index</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>N/A</td>
<td>100%</td>
<td>(N/A)</td>
</tr>
</tbody>
</table>

---

*Note.* Tied ranks (i.e., duplicate values) were common within each centrality index, and enabled nodes to have multiple possible ranks; a match was counted if a symptom could have an identical unique rank-order (e.g., fifth) in both samples. Mismatches were only counted if there was no possible combination of rank-orders that simultaneously facilitated a match and maintained a numerically ordered set of values.

N/A is indicated for the range where all results across the ten sets of split-halves analyses were identical.

---

<table>
<thead>
<tr>
<th>Centrality Index</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>N/A</td>
<td>100%</td>
<td>(N/A)</td>
</tr>
</tbody>
</table>

---

<table>
<thead>
<tr>
<th>Centrality Index</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(.21–.77)</td>
<td>(38.9–66.7)</td>
<td>(.30–1.00)</td>
</tr>
</tbody>
</table>

---

*No node ranked as most central for at least two centrality indices*

*All of the nodes had an estimated centrality index of 0.*

*At least 16 (89%) of nodes had an estimated centrality index of 0.*

---

*Note.* Tied ranks (i.e., duplicate values) were common within each centrality index, and enabled nodes to have multiple possible ranks; a match was counted if a symptom could have an identical unique rank-order (e.g., fifth) in both samples. Mismatches were only counted if there was no possible combination of rank-orders that simultaneously facilitated a match and maintained a numerically ordered set of values.

---

N/A is indicated for the range where all results across the ten sets of split-halves analyses were identical.
Table 4. Summary of the Comparisons between the Ten Pairs of Random Split-Halves from the National Survey of Mental Health and Wellbeing; Median (Range)

<table>
<thead>
<tr>
<th>Network Characteristics</th>
<th>Association Networks</th>
<th>Regularized Ising Models</th>
<th>Censored Relative Importance Networks</th>
<th>Directed Acyclic Graphs</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Connectivity (% possible edges)</td>
<td>100% (N/A)</td>
<td>100% (N/A)</td>
<td>47.7% (43.1–48.4)</td>
<td>45.8% (43.1–48.4)</td>
</tr>
<tr>
<td>Density</td>
<td>.79 (.78–.80)</td>
<td>.79 (.78–.79)</td>
<td>1.18 (1.14–1.25)</td>
<td>1.22 (1.12–1.33)</td>
</tr>
</tbody>
</table>

| Changes in Estimated Edges |                      |                          |                                       |                        |
|----------------------------|----------------------|--------------------------|---------------------------------------|                        |
| Mean absolute % change in edge weights of replicated edges | 1.3% (1.1–2.1) | 48.4% (36.8–68.7) | 6.8% (5.7–8.6) | N/A |
| Proportion of edges that replicated from the first random half to the second | 100% (N/A) | 83.4% (78.1–89.4) | 85.4% (76.7–96.3) | 52.9% (36.8–61.5) |
| Edges that failed to replicate from the first random half | 0% (N/A) | 16.6% (10.6–21.9) | 14.6% (3.7–23.3) | 47.1% (38.5–63.2) |
| Edges unique to the second random half | 0% (N/A) | 13.0% (11.9–16.9) | 8.0% (0–20.7) | 46.4% (28.1–65.8) |

<table>
<thead>
<tr>
<th>Node Centrality</th>
<th>% matched</th>
<th># most central</th>
<th>% matched</th>
<th># most central</th>
<th>% matched</th>
<th># most central</th>
<th>% matched</th>
<th># most central</th>
</tr>
</thead>
<tbody>
<tr>
<td>Same most central node in both split-halves</td>
<td>30%</td>
<td>3</td>
<td>0%</td>
<td>2</td>
<td>N/A</td>
<td>0</td>
<td>0%</td>
<td>4</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Rank-order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
<th>Correlation</th>
<th>Matches in Rank-Order</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strength/Out Strength/Out Degree</td>
<td>.79 (.74–.84)</td>
<td>25.0% (5.6–38.9)</td>
<td>.78 (.61–.84)</td>
<td>33.3% (16.7–44.4)</td>
<td>.76 (.70–.89)</td>
<td>55.6% (44.4–61.1)</td>
<td>.39 (.07–.59)</td>
<td>36.1% (16.7–55.6)</td>
</tr>
</tbody>
</table>
**In Strength/In Degree**

<table>
<thead>
<tr>
<th></th>
<th>N/A</th>
<th>N/A</th>
<th>N/A</th>
<th>N/A</th>
<th>.83</th>
<th>55.6%</th>
<th>.44</th>
<th>44.4%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>N/A</td>
<td>N/A</td>
<td>.79–92</td>
<td>38.9–66.7</td>
<td>.15–.80</td>
<td>22.2–55.6</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Closeness**

<table>
<thead>
<tr>
<th></th>
<th>.76</th>
<th>25.0%</th>
<th>.58</th>
<th>16.7%</th>
<th>N/A</th>
<th>100%</th>
<th>1.00</th>
<th>100%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(.74–.91)</td>
<td>(11.1–38.9%)</td>
<td>(.37–.80)</td>
<td>(0–27.8)</td>
<td>N/A</td>
<td>(N/A)</td>
<td>(-.06–1.00)</td>
<td>(88.9–100)</td>
</tr>
</tbody>
</table>

**Betweenness**

<table>
<thead>
<tr>
<th></th>
<th>N/A</th>
<th>100%</th>
<th>.57</th>
<th>52.8%</th>
<th>.58</th>
<th>94.4%</th>
<th>.24</th>
<th>13.9%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(N/A)</td>
<td>(N/A)</td>
<td>(N/A)</td>
<td>(N/A)</td>
<td>(N/A)</td>
<td>(N/A)</td>
<td>(N/A)</td>
<td>(N/A)</td>
</tr>
</tbody>
</table>

|               | (.44–.81)| (38.9–72.2)| (.32–1.00)| (88.9–100)| (-.07–.36)| (5.6–38.9)|

---

**Note.** Tied ranks (i.e., duplicate values) were common within each centrality index, and enabled nodes to have multiple possible ranks; a match was counted if a symptom could have an identical unique rank-order (e.g., fifth) in both samples. Mismatches were only counted if there was no possible combination of rank-orders that simultaneously facilitated a match and maintained a numerically ordered set of values. N/A is indicated for the range where all results across the ten sets of split-halves analyses were identical.

---

a No node ranked as most central for at least two centrality indices
b All of the nodes had an estimated centrality index of 0.

At least 16 (89%) of nodes had an estimated centrality index of 0 in all split-halves.
Figure Captions

**Figure 1.** An illustrative example of the variance that is used to calculate association networks (left); and concentration networks, relative important networks, and directed acyclic graphs (right).

**Figure 2.** Association networks based on tetrachoric correlations. NCS-R = National Comorbidity Survey – Replication; NSMHWB = National Survey of Mental Health and Wellbeing. See Table 1 for symptom abbreviations.

**Figure 3.** Regularized Ising models. NCS-R = National Comorbidity Survey – Replication, NSHWB = National Survey of Mental Health and Wellbeing. The following edges are negative in NCS-R: gSle–mFat, gCon–mFat, and gFat–moto. All other edges are positive, and the line weights represent the strength of the relationship between two nodes. See Table 1 for symptom abbreviations.

**Figure 4.** Censored relative importance networks. The network represents the edges that highlight which nodes have higher relative importance as predictors in the model: Edges were only estimated if they represented an $R^2$ of at least 5% (i.e., an edge weight of .05) and had at least .5% stronger relative importance than the other edge in the node pair. The line weights represent the strength of the relationships, and the arrows represent the direction. NCS-R = National Comorbidity Survey – Replication, NSHWB = National Survey of Mental Health and Wellbeing. See Table 1 for symptom abbreviations.

**Figure 5.** Directed acyclic graphs (DAGs) based on a hill-climbing algorithm for NCS-R (left) and NSMHWB (right). Note that these DAGs are presented in a tree format where nodes are positioned according to their predictive power, as all “causal” arrows point downwards; nodes at the top of the graph predict the nodes lower in the graph (but the reverse is not true). GAD symptoms are presented in blue, and MDE symptoms are presented in red. Symptom abbreviations for each disorder are also listed in Table 1. NCS-R = National
Comorbidity Survey – Replication; NSMHWB = National Survey of Mental Health and Wellbeing; GAD = generalized anxiety disorder; MDE = major depressive episode.
Figure 1

Variance used to estimate the network

Variance used from the relationship between A and B to estimate the edge A–B
REPLICABILITY OF PSYCHOPATHOLOGY NETWORKS

Figure 2
Figure 3

NCS-R

NSMHWB
Figure 4
Figure 5
Appendix S1: Exploring the Sensitivity of Conditional Independence Networks to Multiple Types of Change

Here are four correlated variables: A, B, C, and D

Each circle represents all of the information (or variance) we have about a symptom that was measured in a survey. For example, A could represent the mean level and variability of the symptom “feeling on edge” in our data.

The overlap between any pair of symptoms represents the relationship between them. For example, the darker shaded area here shows the shared variance (“covariance”) or correlation between A and B.

In this example we are interested in symptoms of anxiety, and have measured:
- Feeling on edge
- Frequency of worrying
- Difficulty controlling worries
- Difficulty falling asleep
Understanding the Variance Used in Network Analyses

We might analyze the relationships between these four symptoms to get a better understanding of the disorder or syndrome that they relate to. For example, if we think of these symptoms as measuring the construct of *anxiety* then we might want to look more closely at where they overlap (i.e., where we think we have measured *anxiety* more reliably; see Panel 2 below).

- **Factor analysis** uses this information to define a latent variable to represent *anxiety*.
- **Association networks** represent the overlap between each pair of symptoms as an edge between them to illustrate the series of relationships between pairs of symptoms.

On the other hand, if we wanted to look at the *unique* relationships between pairs of symptoms (i.e., where two symptoms overlap with each other, but not with any other symptoms) then we would focus on the areas of covariance highlighted in Panel 3. These areas are *conditionally independent* relationships, which we could summarize as, for example, “the relationship between A and B, after controlling for C and D.”

- **Conditional independence networks**, including **concentration networks**, **relative importance networks**, and **directed acyclic networks** use this information to illustrate the *unique* and speculatively *causal* relationships between pairs of symptoms.

In short:
Extending the Example to Eight Symptoms

Say we measure four more symptoms of anxiety (E, F, G, and H), for example:

- Worrying about lots of different topics
- Difficulty concentrating
- Feeling more fatigued than usual
- Irritability

An updated version of the variance used in the analyses looks like this:

On the left, _anxiety_ is being measured more reliably (darker areas = more reliability in the measurement), and we are still using all of the relationships between pairs of variables.

On the right, much less variance is being used to calculate the model. A and B have no _unique_ relationship, so they will not be related to each other in conditional independence networks. It is also interesting to consider whether the variance used from symptom A is meaningful in any real-world sense.
A Small Change in G

What would happen if—in another sample—G had a slightly different relationship with the other symptoms?

In this example, we held the relationships for A–F to be exactly equal, and only shifted their relationship with G (e.g., G is more related to B and less related to C in Sample 2). This is an artificial example for illustration, as the interrelationships among all nodes would be expected to vary slightly between two samples.

Here is an indication of how the relationships in the networks would compare:

While the information used in the association networks remains largely stable—particularly in the more reliably measured areas—there are four noteworthy changes (six total) in the information used to calculate the other network models:

- G now has a relationship with F included in the calculation of the model, while the relationship of B:F is 2-3 times smaller.
- Similarly, B now has a relationship with C included in the calculation of the model, and the relationship of G:C is 3-4 times smaller.
Adding Another Symptom to the Model

What would happen if we measured another related item, I (muscle aches or soreness, for example)?

Here is how the old and new relationships would compare:

With I, we now have some more reliability in the variance in the association networks.

In contrast, the relationships in the conditional independence networks shift. Specifically, A:E is now excluded from the conditional independence networks (despite their substantial overlap); D:E is also excluded from the model; D:H is substantially reduced in size; and there are three new relationships included in the calculation of the model (D:I, H:I, and a substantial relationship for I:E).
Removing a Symptom from the Model

Finally, what would happen if we had not thought to measure A?

Here is how the old and new relationships would compare:

As we have seen above, A has very little unique influence in the model, but leaving it out will reduce the reliability of measurement for association networks.

In the conditional independence networks there are two substantial changes (six total) in the information used to calculate the models. Namely, the relationships between E:F and D:E will be substantially larger.
Overall, we see along the top row of the figure above that the relationships included in the association networks are largely stable with each change.

In contrast, note that each self-contained area along the bottom panel is the basis of the calculation of an edge in the conditional independence networks. These areas are very sensitive to change—growing, shrinking, appearing and disappearing with each change in the data.

In summary, it is clear that conditionally independent relationships among items—particularly those that incorporate substantial measurement error—are likely to be unstable with even subtle changes in the data or model.
Figure S1. Uncensored relative importance networks with 306 edges. Note that many of the edges between the disorders are so small that it is difficult to see them. NCS-R = National Comorbidity Study – Replication; NSMHWB = National Survey of Mental Health and Wellbeing. See Table 1 for symptom abbreviations.
**Figure S2.** Directed acyclic graphs plotted using the Fruchterman and Reingold (1991) algorithm. NCS-R = National Comorbidity Study – Replication; NSMHWB = National Survey of Mental Health and Wellbeing. See Table 1 for symptom abbreviations.